

**Time : 2 Hrs.**

**Marks : 40**

**Ans.** Option d.

$$V + F - E = 2$$

- 2) To draw a tangent to a circle without using its centre we use .....
- inscribed angle theorem
  - isosceles triangle theorem
  - property of alternate angle test
  - property of angles in alternate segment

**Ans.** Option (d)

- 3) The longest chord of a circle is 7.8 cm. What is the radius of the circle?
- 3.9
  - 7.8
  - 15.6
  - 8

**Ans.** Option a.

**Hint :**  $r = \frac{d}{2}$

- 4) Slope of a line parallel to x-axis is .....
- Zero
  - One
  - Not defined
  - None of these

**Ans.** Option a.

**B) Solve the following questions.**

**(4)**

- 1) If  $\sin\theta = \frac{20}{29}$  then find  $\cos\theta$

**Ans.**  $\sin^2\theta + \cos^2\theta = 1$

$$\left(\frac{20}{29}\right)^2 + \cos^2\theta = 1$$

$$\frac{400}{841} + \cos^2\theta = 1$$

$$\cos^2\theta = 1 - \frac{400}{841}$$

$$= \frac{441}{841}$$

Taking square root of both sides.

$$\cos\theta = \frac{21}{29}$$

- 2) Show that points P(- 2, 3), Q(1, 2), R(4, 1) are collinear.

**Ans.** P(- 2, 3), Q(1, 2) and R(4, 1) are given points

$$\text{slope of line PQ} = \frac{Y_2 - Y_1}{X_2 - X_1} = \frac{2 - 3}{1 - (-2)} = \frac{-1}{3}$$

$$\text{Slope of line QR} = \frac{Y_2 - Y_1}{X_2 - X_1} = \frac{1 - 2}{4 - 1} = \frac{-1}{3}$$

Slope of line PQ and line QR is equal.

But point Q lies on both the lines.

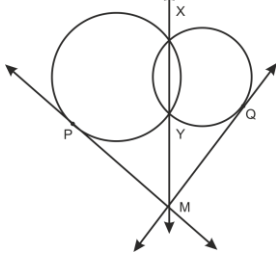
$\therefore$  Point P, Q, R are collinear.

- 3) Ratio of corresponding sides of two similar triangles is 4:7 then find the ratio of their areas = ?

**Ans.** By theorem of areas of similar triangles,  
 Ratio of areas of the given triangles =  $\left(\frac{4}{7}\right)^2 = \frac{16}{49} = 16:49$

∴ The ratio of areas is 16:49.

- 4) In figure, two circles intersect each other in points X and Y. Tangents drawn from a point M on line XY touch the circles at P and Q. Prove that, seg PM ≅ seg QM.



**Ans.** Line MX is a common secant of the two circles.

∴  $PM^2 = MY \times MX$  ... (i)

Similarly  $QM^2 = MY \times MX$ , tangent secant segment theorem... (ii)

∴ From (i) and (ii)  $PM^2 = QM^2$

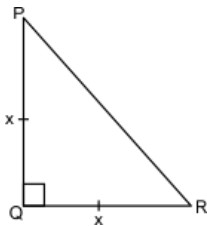
∴  $PM = QM$

seg PM ≅ seg QM

**Q.2 A) Complete the following Activities. (Any two)**

(4)

- 1) A side of an isosceles right angled triangle is x. Find its hypotenuse.



In  $\triangle PQR$ ,  $\angle PQR = 90^\circ$

and  $PQ = QR = x$

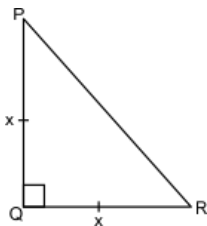
∴  $PR^2 = \underline{\hspace{2cm}}$  ... [Pythagoras theorem]  
 $= \underline{\hspace{2cm}}$

∴  $PR^2 = \underline{\hspace{2cm}}$

∴  $PR = \underline{\hspace{2cm}}$  units ... [Taking square root]

∴ The length of hypotenuse is  $\underline{\hspace{2cm}}$  units.

**Ans.** A side of an isosceles right angled triangle is x. Find its hypotenuse.



In  $\triangle PQR$ ,  $\angle PQR = 90^\circ$

and  $PQ = QR = x$

∴  $PR^2 = PQ^2 + QR^2$  ... [Pythagoras theorem]  
 $= x^2 + x^2$

∴  $PR^2 = 2x^2$

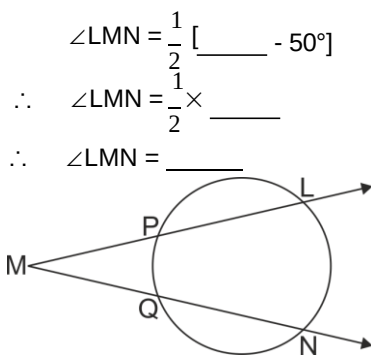
∴  $PR = \sqrt{2}x$  units ... [Taking square root]

∴ The length of hypotenuse is  $\sqrt{2}x$  units.

- 2) In the figure  $m(\text{arc LN}) = 110^\circ$ ,  $m(\text{arc PQ}) = 50^\circ$  then complete the following activity to find  $\angle LMN$ .

$\angle LMN = \frac{1}{2} [m(\text{arc LN}) - [\underline{\hspace{2cm}}]]$

∴



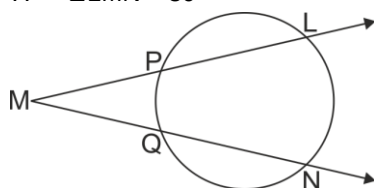
**Ans.** In the figure  $m(\text{arc LN}) = 110^\circ$ ,  $m(\text{arc PQ}) = 50^\circ$  then complete the following activity to find  $\angle LMN$ .

$$\angle LMN = \frac{1}{2} [m(\text{arc LN}) - m(\text{arc PQ})]$$

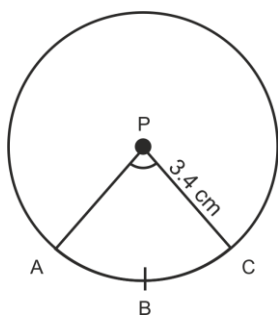
$$\therefore \angle LMN = \frac{1}{2} [110^\circ - 50^\circ]$$

$$\therefore \angle LMN = \frac{1}{2} \times 60^\circ$$

$$\therefore \angle LMN = 30^\circ$$



3)



In figure, radius of circle is 3.4 cm and perimeter of sector P-ABC is 12.8 cm. Find  $A(P\text{-}ABC)$ .

Given : Radius of circle =  $r = 3.4$  cm  
 Perimeter of sector = 12.8 cm  
 : Perimeter = length of the arc +  $2r$

$$\therefore \text{Length of arc} = 12.8 - 2 \times 3.4$$

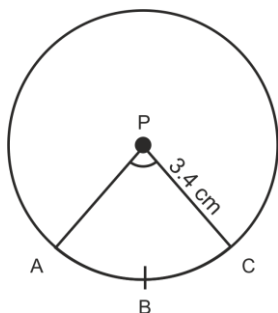
$$\therefore l = 12.8 - 6.8$$

$$\therefore l = \quad \text{cm}$$

area of sector =  $\quad$   
 $= \quad$   
 $= 3 \times 3.4$   
 $= \quad \text{cm}^2$

$A(P\text{-}ABC)$  is  $\quad \text{cm}^2$

**Ans.**



In figure, radius of circle is 3.4 cm and perimeter of sector P-ABC is 12.8 cm. Find  $A(P\text{-}ABC)$ .

Given : Radius of circle =  $r = 3.4$  cm  
 Perimeter of sector = 12.8 cm  
 : Perimeter = length of the arc +  $2r$

$$\therefore \text{Length of arc} = 12.8 - 2 \times 3.4$$

$$\therefore l = 12.8 - 6.8$$

$$\therefore l = 6.0 \text{ cm}$$

$$\text{area of sector} = \frac{\text{length of the arc} \times \text{radius}}{2}$$

$$= \frac{6 \times 3.4}{2}$$

$$= 3 \times 3.4$$

$$= 10.2 \text{ cm}^2$$

A(P-ABC) is  $10.2 \text{ cm}^2$

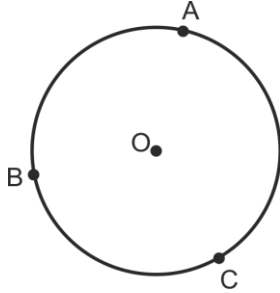
**B) Solve the following questions. (Any four)**

**(8)**

**1)** A, B, C are any points on the circle with centre O.

(i) Write the names of all arcs formed due to these points.

(ii) If  $m \text{ arc}(BC) = 110^\circ$  and  $m \text{ arc}(AB) = 125^\circ$ , find measures of all remaining arcs.



**Ans.** (i) Names of arcs -

arc AB, arc BC, arc AC, arc ABC, arc ACB, arc BAC

$$(ii) m(\text{arc ABC}) = m(\text{arc AB}) + m(\text{arc BC})$$

$$= 125^\circ + 110^\circ = 235^\circ$$

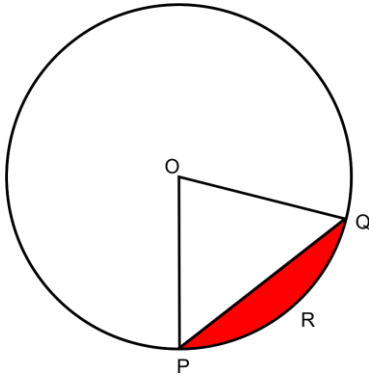
$$m(\text{arc AC}) = 360^\circ - m(\text{arc ACB})$$

$$= 360^\circ - 235^\circ = 125^\circ$$

$$\text{Similarly, } m(\text{arc ACB}) = 360^\circ - 125^\circ = 235^\circ$$

$$\text{and } m(\text{arc BAC}) = 360^\circ - 110^\circ = 250^\circ$$

**2)** In the figure, if O is the centre of the circle, PQ is a chord.  $\angle POQ = 90^\circ$ , area of shaded region is  $114 \text{ cm}^2$ , find the radius of the circle. ( $\pi = 3.14$ )



**Ans.** Area of shaded region  $= r^2 \left( \frac{\pi\theta}{360} - \frac{\sin\theta}{2} \right)$

$$= r^2 \left( \frac{\pi \times 90}{360} - \frac{\sin 90}{2} \right) \dots \because \theta = 90^\circ \text{ Area of shaded region} = 114 \text{ cm}^2$$

$$114 = r^2 \left( \frac{\pi}{4} - \frac{1}{2} \right)$$

$$114 = r^2 \left( \frac{\pi - 2}{4} \right)$$

$$114 \times 4 = r^2 (1.14)$$

$$r^2 = \frac{114 \times 4}{1.14}$$

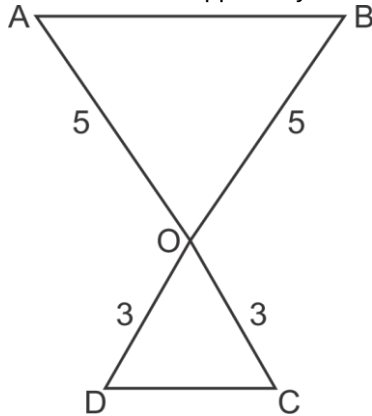
$$r^2 = 4 \times 100$$

$\therefore$

$$\boxed{r = 20 \text{ cm}}$$

**3)** In the following figure, indicate whether the triangle are similar or not.

Give reason in support of your answer.



**Ans. Proof:**

(1)  $AO = 5, CO = 3$  ... (Given)

$$\therefore \frac{AO}{CO} = \frac{5}{3}$$

(2)  $BO = 5, DO = 3$  ... (Given)

$$\therefore \frac{BO}{DO} = \frac{5}{3}$$

(3) In  $\triangle AOB$  and  $\triangle COD$

For  $AOB \leftrightarrow COD$

$$\frac{AO}{CO} = \frac{BO}{DO} \quad \dots \text{[From (1) and (2)]}$$

$$\therefore \angle AOB \cong \angle COD \quad \dots \text{(Vertically opposite angles)}$$

$$\therefore \triangle AOB \sim \triangle COD \quad \dots \text{(S - A - S Test of similarity)}$$

4) If  $A(3, 5)$ ,  $B(7, 9)$  and point Q divides seg AB in the ratio 2 : 3 then find co-ordinates of point Q.

**Ans.** In the given example let  $(x_1, y_1) = (3, 5)$

and  $(x_2, y_2) = (7, 9)$ .

$m : n = 2 : 3$

According to section formula,

$$x = \frac{mx_2 + nx_1}{m + n} = \frac{2 \times 7 + 3 \times 3}{2 + 3} = \frac{23}{5}, \quad y = \frac{my_2 + ny_1}{m + n} = \frac{2 \times 9 + 3 \times 5}{2 + 3} = \frac{33}{5}$$

$\therefore$  Co-ordinates of Q are  $\left(\frac{23}{5}, \frac{33}{5}\right)$

5) In  $\triangle LMN$ ,  $l = 5$ ,  $m = 13$ ,  $n = 12$ . State whether  $\triangle LMN$  is a right-angled triangle or not.

**Ans.**  $LM = 5, MN = 13, LN = 12$

$$LM^2 = 25, MN^2 = 169, LN^2 = 144$$

$$\therefore 169 = 144 + 25$$

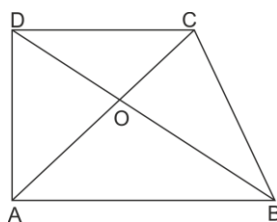
$$\therefore MN^2 = LN^2 + LM^2$$

$\therefore$  By Converse of Pythagoras theorem  $\triangle LMN$  is a right angled triangle.

**Q.3 A) Complete the following activity. (Any one)**

(3)

1)



In the given figure, ABCD is a trapezium in which  $AB \parallel DC$ . If  $2AB = 3DC$ , find the ratio of the areas of  $\triangle AOB$  and  $\triangle COD$ .

$$\frac{AB}{DC} = \frac{3}{2}$$

To find : area  $\triangle AOB$  : area of  $\triangle COD$

Proof : In  $\triangle AOB$  and  $\triangle COD$

$$\angle AOB = \angle COD$$

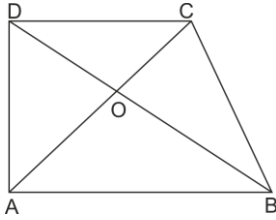
$$\angle OAB = \angle OCD$$

(alternate angles)

$$\therefore \frac{\text{area } \triangle AOB}{\text{area } \triangle COD} = \frac{3^2}{2^2} = \frac{9}{4}$$

Ratio in the areas of  $\triangle AOB$  and  $\triangle COD$  9 : 4

Ans.



In the given figure, ABCD is a trapezium in which  $AB \parallel DC$ . If  $2AB = 3DC$ , find the ratio of the areas of  $\triangle AOB$  and  $\triangle COD$ .

$$\frac{AB}{DC} = \frac{3}{2}$$

To find : area  $\triangle AOB$  : area of  $\triangle COD$

Proof : In  $\triangle AOB$  and  $\triangle COD$

$$\angle AOB = \angle COD$$

(vertically opposite angles)

$$\angle OAB = \angle OCD$$

(alternate angles)

$$\therefore \triangle AOB \sim \triangle COD$$

(AA axiom)

$$\therefore \frac{\text{area } \triangle AOB}{\text{area } \triangle COD} = \frac{AB^2}{DC^2} = \frac{3^2}{2^2} = \frac{9}{4}$$

Ratio in the areas of  $\triangle AOB$  and  $\triangle COD$  **9 : 4**

- 2) Some plastic balls of radius 1 cm were melted and cast into a tube. The thickness, length and outer radius of the tube were 2 cm, 90 cm and 30 cm respectively. How many balls were melted to make the tube?

$$\text{Tube} = \text{cylinder}$$

$$\text{Radius} = \text{Outer radius} - \text{Thickness}$$

$$\therefore = 30 - 2$$

$$\therefore = 28 \text{ cm}$$

$$\text{Number of balls} = \frac{\text{Volume of tube}}{\text{Volume of ball}}$$

$$\therefore = \frac{\pi(r_1^2 - r_2^2)h}{\frac{4}{3}\pi r^3}$$

$$\therefore = \frac{(900 - 784) \times 90 \times 3}{4}$$

$$\therefore = \frac{(900 - 784) \times 90 \times 3}{4}$$

$$\therefore = 7830$$

- Ans. Some plastic balls of radius 1 cm were melted and cast into a tube. The thickness, length and outer radius of the tube were 2 cm, 90 cm and 30 cm respectively. How many balls were melted to make the tube?

$$\text{Tube} = \text{cylinder}$$

$$\text{Radius} = \text{Outer radius} - \text{Thickness}$$

$$\therefore = 30 - 2$$

$$\therefore = 28 \text{ cm}$$

$$\text{Number of balls} = \frac{\text{Volume of tube}}{\text{Volume of ball}}$$

$$\therefore = \frac{\pi(r_1^2 - r_2^2)h}{\frac{4}{3}\pi r^3}$$

$$\therefore = \frac{((30)^2 - (28)^2) \times 90}{\frac{4}{3} \times (1)^3}$$

$$\therefore = \frac{(900 - 784) \times 90 \times 3}{4}$$

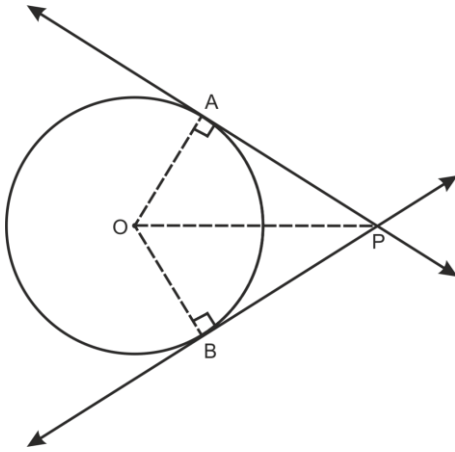
$$\therefore = \frac{(900 - 784) \times 90 \times 3}{4}$$

$$\therefore = 7830 \text{ balls}$$

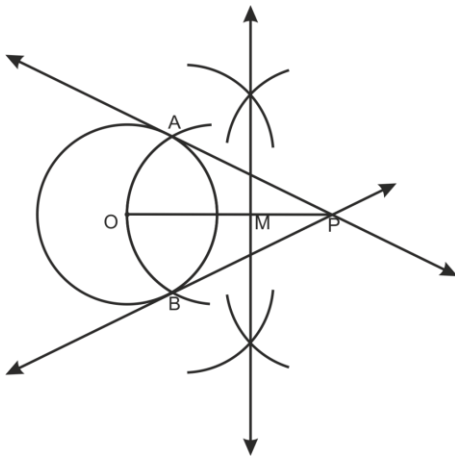
B) Solve the following questions. (Any two)

- 1) Construct tangents to a circle from a point outside the circle.

Ans.



Let P be a point in the exterior of the circle. Let PA and PB be the tangents to the circle with the centre O, touching the circle in points A and B respectively.



- 2) If point  $(x, y)$  is equidistant from points  $(7, 1)$  and  $(3, 5)$ , show that  $y = x - 2$ .

Ans. Let point P  $(x, y)$  be equidistant from points A  $(7, 1)$  and B  $(3, 5)$

$$\begin{aligned} \therefore AP &= BP \\ \therefore AP^2 &= BP^2 \\ \therefore (x - 7)^2 + (y - 1)^2 &= (x - 3)^2 + (y - 5)^2 \\ \therefore x^2 - 14x + 49 + y^2 - 2y + 1 &= x^2 - 6x + 9 + y^2 - 10y + 25 \\ \therefore -8x + 8y &= -16 \\ \therefore x - y &= 2 \\ \therefore y &= x - 2 \end{aligned}$$

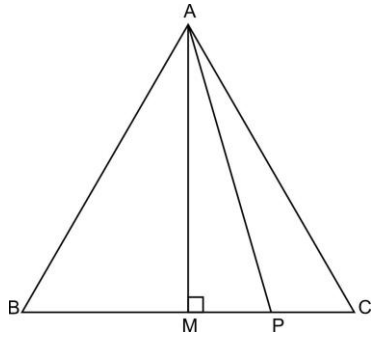
- 3) Prove that  $\frac{\sin \theta - 2 \sin^3 \theta}{2 \cos^3 \theta - \cos \theta} = \tan \theta$

Ans. Proof: LHS =  $\frac{\sin \theta - 2 \sin^3 \theta}{2 \cos^3 \theta - \cos \theta}$

$$\begin{aligned} &= \frac{\sin \theta (1 - 2 \sin^2 \theta)}{\cos \theta (2 \cos^2 \theta - 1)} \\ &= \frac{\sin \theta (\sin^2 \theta + \cos^2 \theta - 2 \sin^2 \theta)}{\cos \theta (2 \cos^2 \theta - \sin^2 \theta - \cos^2 \theta)} \quad \dots (\sin^2 \theta + \cos^2 \theta = 1) \\ &= \frac{\sin \theta (\cos^2 \theta - \sin^2 \theta)}{\cos \theta (\cos^2 \theta - \sin^2 \theta)} \\ &= \frac{\sin \theta}{\cos \theta} \\ &= \tan \theta = \text{RHS} \\ \therefore \frac{\sin \theta - 2 \sin^3 \theta}{2 \cos^3 \theta - \cos \theta} &= \tan \theta \end{aligned}$$

- 4)  $\triangle ABC$  is an equilateral triangle. Point P is on base BC such that  $PC = \frac{1}{3}BC$ , if  $AB = 6$  cm find AP.

Ans.



Draw seg  $AM \perp$  side BC such that B-M-C

$\triangle ABC$  is equilateral triangle.

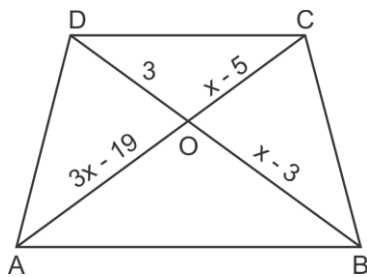
- $\therefore AB = BC = AC = 6$ cm ... (Sides of an equilateral triangle) ... (1)  
 $\angle C = 60^\circ$  ... (Sides of an equilateral triangle) ... (2)  
 In  $\triangle AMC$ ,  
 $\angle AMC + \angle ACM + \angle MAC = 180^\circ$  ... (Sum of all angles of a triangle is  $180^\circ$ )  
 $\therefore 90^\circ + 60^\circ + \angle MAC = 180^\circ$  ... (From (1) and (2))  
 $\therefore 150 + \angle MAC = 180^\circ$   
 $\therefore \angle MAC = 180^\circ - 150^\circ$   
 $\therefore \angle MAC = 30^\circ$   
 $\therefore \triangle AMC$  is a  $30^\circ$ - $60^\circ$ - $90^\circ$  triangle  
 $\therefore$  by  $30^\circ$ - $60^\circ$ - $90^\circ$  triangle theorem  
 $AM = \frac{\sqrt{3}}{2}AC$  ... (Side opposite to  $60^\circ$ )  
 $\therefore AM = \frac{\sqrt{3}}{2} \times 6$  ... [From (1)]  
 $\therefore AM = 3\sqrt{3}$ cm  
 $MC = \frac{1}{2}BC$  ... (Side opposite to  $30^\circ$ )  
 $\therefore MC = \frac{1}{2} \times 6$  ... [From (1)]  
 $\therefore MC = 3$ cm  
 $PC = \frac{1}{3}BC$  ... (Given)  
 $\therefore PC = \frac{1}{3} \times 6$  ... [From (1)]  
 $\therefore PC = 2$ cm  
 $MP + PC = MC$  (M-P-C)  
 $\therefore MP + 2 = 3$   
 $\therefore MP = 3 - 2$   
 $\therefore MP = 1$ cm  
 In  $\triangle AMP$ ,  
 $\angle AMP = 90^\circ$  ... (Construction)  
 $\therefore$  by Pythagoras theorem,  
 $AP^2 = AM^2 + MP^2$   
 $\therefore AP^2 = (3\sqrt{3})^2 + 1^2$   
 $\therefore AP^2 = 27 + 1$   
 $\therefore AP^2 = 28$   
 $\therefore AP^2 = 4 \times 7$   
 $\therefore AP = 2\sqrt{7}$ cm ... (Taking square roots on both the sides)  
 $\therefore AP = 2\sqrt{7}$ cm

Q.4 Solve the following questions. (Any two)

(8)

- 1) In the figure, seg  $AB \parallel$  seg  $DC$ . Using the information given find the value of x.



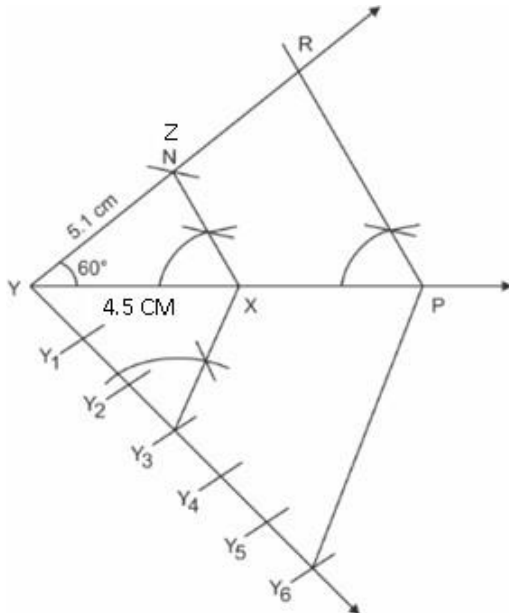


- Ans.** (1) In  $\square ABCD$ ,  
 seg  $AB \parallel$  seg  $DC$  ... (given)  
 $\therefore \angle DCA \cong \angle BAO$  ... (Alternate angles for transversal AC)  
 i.e.  $\angle DCO \cong \angle BAO$  ... (A-O-C)  
 (2) In  $\triangle DOC$  and  $\triangle BOA$   
 (a)  $\angle DCO \cong \angle BAO$  ... [from (1)]  
 (b)  $\angle DOC \cong \angle BOA$  ... (vertically opposite angles)  
 (c)  $\therefore \triangle DOC \sim \triangle BOA$  ... (A - A test of similarity)  
 (3)  $\frac{DO}{AO} = \frac{CO}{BO}$  ... (c.s.s.t)  
 (4) But  $DO = 3$ ,  $BO = x - 3$   
 $CO = x - 5$ ,  $AO = 3x - 19$  ... (given)  
 (5)  $\therefore \frac{3}{x - 3} = \frac{x - 5}{3x - 19}$  ... [from (3) and (4)]  
 $\therefore 3(3x - 19) = (x - 5)(x - 3)$   
 $9x - 57 = x^2 - 8x + 15$   
 $\therefore x^2 - 8x - 9x + 15 + 57 = 0$   
 $\therefore x^2 - 17x + 72 = 0$   
 $\therefore (x - 8)(x - 9) = 0$   
 either  $x - 8 = 0$  or  $x - 9 = 0$   
 $\therefore x = 8$  or  $x = 9$

The value of  $x = 8$  or  $x = 9$

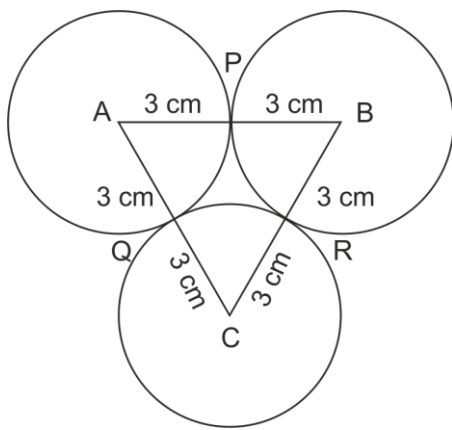
- 2)  $\triangle XYZ \sim \triangle PYR$ ; In  $\triangle XYZ$ ,  $\angle Y = 60^\circ$ ,  $XY = 4.5$  cm,  $YZ = 5.1$  cm and  $\frac{XY}{PY} = \frac{4}{7}$  Construct  $\triangle XYZ$  and  $\triangle PYR$ .

**Ans.**



- 3) Draw circles with centres A, B and C each of radius 3 cm, such that each circle touches the other two circles.

**Ans.**



Analysis : Let the circles with centres A, B and C touch at points P, R and Q as shown.

By theorem of touching circles, we get A–P–B, B–R–C and A–Q–C.

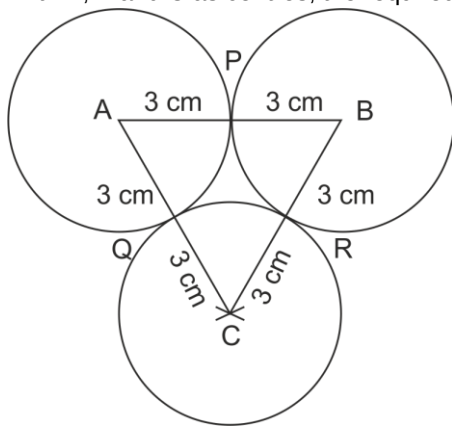
$$\therefore AB = AP + PB = 3 + 3 = 6 \text{ cm.}$$

Similarly BC = 6 cm and AC = 6 cm

$\therefore$  We can construct  $\triangle ABC$  with

$$AB = BC = AC = 6 \text{ cm}$$

With A, B and C as centres, the required circles of radius 3 cm can be drawn.



#### Q.5 Solve the following questions. (Any one)

(3)

- 1) The diameter and length of a roller is 120 cm and 84 cm respectively. To level the ground, 200 rotations of the roller are required. Find the expenditure to level the ground at the rate of Rs. 10 per sq.m.

**Ans.** Given : diameter of rollers = 120 cm = 1.2m  
 $\therefore$  radius of roller = 60 cm = 0.6 m  
length = height of roller = 84 cm = 0.84m  
rate of levelling = Rs. 10 per  $\text{m}^2$   
No. of rotations = 200

To find : Total cost of levelling

Solution:

$$\text{Curved Surface Area of Roller} = 2\pi rh$$

$$= 2 \times \frac{22}{7} \times 0.6 \times 0.84$$

$$= 3.168 \text{m}^2$$

One rotation of roller will cover  $3.168 \text{m}^2$  of area, but total rotations 200 are made.

$$\therefore \text{Total area levelled} = 200 \times 3.168 = \text{Rs. } 633.6 \text{m}^2$$

$$\text{The cost of levelling is Rs. } 633.6 \times 10 = \text{Rs. } 6336$$

- 2) **Prove :**  $\frac{\operatorname{cosec} \theta}{\operatorname{cosec} \theta - 1} + \frac{\operatorname{cosec} \theta}{\operatorname{cosec} \theta + 1} = 2 \sec^2 \theta$

**Ans. Proof:** LHS =  $\frac{\operatorname{cosec} \theta}{\operatorname{cosec} \theta - 1} + \frac{\operatorname{cosec} \theta}{\operatorname{cosec} \theta + 1}$   

$$= \frac{\operatorname{cosec} \theta (\operatorname{cosec} \theta + 1) + \operatorname{cosec} \theta (\operatorname{cosec} \theta - 1)}{(\operatorname{cosec} \theta - 1)(\operatorname{cosec} \theta + 1)}$$
  

$$= \frac{\operatorname{cosec}^2 \theta + \operatorname{cosec} \theta + \operatorname{cosec}^2 \theta - \operatorname{cosec} \theta}{\operatorname{cosec}^2 \theta - 1}$$

$$\begin{aligned}
&= \frac{2 \operatorname{cosec}^2 \theta}{\operatorname{cosec}^2 \theta - 1} \\
&= \frac{2 (1 + \cot^2 \theta)}{1 + \cot^2 \theta - 1} \\
&= \frac{2 \left( 1 + \frac{1}{\tan^2 \theta} \right)}{\frac{1}{\tan^2 \theta}} \\
&= \frac{2 (\tan^2 \theta + 1)}{\tan^2 \theta} \div \frac{1}{\tan^2 \theta} \\
&= \frac{2 (\sec^2 \theta)}{\tan^2 \theta} \times \tan^2 \theta \\
&= 2 \sec^2 \theta = \text{RHS}
\end{aligned}$$

$$\therefore \frac{\operatorname{cosec} \theta}{\operatorname{cosec} \theta - 1} + \frac{\operatorname{cosec} \theta}{\operatorname{cosec} \theta + 1} = 2 \sec^2 \theta$$

$$\ldots (\operatorname{cosec}^2 \theta = 1 + \cot^2 \theta)$$

$$\ldots \left( \cot \theta = \frac{1}{\tan \theta} \right)$$

$$\ldots (1 + \tan^2 \theta = \sec^2 \theta)$$